## "It's Just Matrix Multiplication" Notation for Weaving <br> Lea Albaugh <br> (@doridoidea)



Hugo Weaving


There are some indications that weaving was already known in the Paleolithic era, as early as 27,000 years ago. An indistinct textile impression has been found at the Dolní Věstonice site. ${ }^{[11]}$ According to the find, the weavers of Upper Palaeolithic were manufacturing a variety of cordage types, produced plaited basketry and sophisticated twined and plain woven cloth. The artifacts include imprints in clay and burned remnants of cloth. ${ }^{[12]}$

The oldest known textiles found in the Americas are remnants of six finely woven textiles and cordage found in Guitarrero Cave, Peru. The weavings, made from plant fibres, are dated between 10100 and 9080 BCE. ${ }^{[13]}$

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6,000 years


Elrond was the son of Eärendil and Elwing, and a great-grandson of Lúthien, born in Beleriand in the First Age, making him well over 6,000 years old by the time of the events described in The Lord of the Rings. Elrond's twin brother was Elros Tar-Minyatur, the first High King of Númenor.

## Elrond - Wikipedia

https://en.wikipedia.org/wiki/Elrond


There are some indications that weaving was already known in the Paleolithic era, as early as 27,000 years ago. An indistinct textile impression has been found at the Dolní Věstonice site. ${ }^{[11]}$ According to the find, the weavers of Upper Palaeolithic were manufacturing a variety of cordage types, produced plaited basketry and sophisticated twined and plain woven cloth. The artifacts include imprints in clay and burned remnants of cloth. ${ }^{[12]}$

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what even is a loom










a weaving draft ("2x2 twill weave")

$$
4
$$

$$
42
$$


tieup

tieup







| Essence of | 1 | $\int_{1 \mathrm{vs} \cdot\left[\begin{array}{l} 1 \\ 2 \\ 9: 52 \end{array}\right]}^{\text {Vectors }}$ | 3BLUE1BROWN SERIES S1-E1 <br> Vectors, what even are they? \| Essence of linear algebra, chapter 1 3Blue1Brown |
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## Grant Sanderson, "3blue1brown"

$$
\begin{gathered}
A=\left[\begin{array}{lll}
1 & 2 & 3 \\
4 & 5 & 6 \\
7 & 8 & 9
\end{array}\right] \\
B=\left[\begin{array}{lll}
10 & 11 & 12 \\
13 & 14 & 15 \\
16 & 17 & 18
\end{array}\right]
\end{gathered}
$$

$A \times B=$
$\left[\begin{array}{lll}10 & 11 & 12 \\ 13 & 14 & 15 \\ 16 & 17 & 18\end{array}\right]$
$\left[\begin{array}{lll}1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9\end{array}\right]$

## $A \times B=$

$\left[\begin{array}{lll}10 & 11 & 12 \\ 13 & 14 & 15 \\ 16 & 17 & 18\end{array}\right]$
$\left[\begin{array}{lll}1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9\end{array}\right][$
I

## $A \times B=$

$$
\begin{gathered}
{\left[\begin{array}{lll}
10 & 11 & 12 \\
13 & 14 & 15 \\
16 & 17 & 18
\end{array}\right]} \\
{\left[\begin{array}{lll}
1 & 2 & 3 \\
4 & 5 & 6 \\
7 & 8 & 9
\end{array}\right]\left[{ }^{(1 \times 10)}\right.}
\end{gathered}
$$

## $A \times B=$

$$
\begin{gathered}
{\left[\begin{array}{lll}
10 & 11 & 12 \\
13 & 14 & 15 \\
16 & 17 & 18
\end{array}\right]} \\
{\left[\begin{array}{lll}
1 & 2 & 3 \\
4 & 5 & 6 \\
7 & 8 & 9
\end{array}\right]}
\end{gathered}\left[\begin{array}{l}
10+(2 \times 13)
\end{array}\right]
$$

## $A \times B=$

$$
\begin{gathered}
{\left[\begin{array}{lll}
10 & 11 & 12 \\
13 & 14 & 15 \\
16 & 17 & 18
\end{array}\right]} \\
{\left[\begin{array}{lll}
1 & 2 & 3 \\
4 & 5 & 6 \\
7 & 8 & 9
\end{array}\right]\left[\begin{array}{l}
10+26+(3 \times 16) \\
\end{array}\right]}
\end{gathered}
$$

## $A \times B=$

$\left[\begin{array}{lll}10 & 11 & 12 \\ 13 & 14 & 15 \\ 16 & 17 & 18\end{array}\right]$

$$
\left[\begin{array}{lll}
1 & 2 & 3 \\
4 & 5 & 6 \\
7 & 8 & 9
\end{array}\right]\left[\begin{array}{l}
84 \\
\end{array}\right.
$$

$A \times B=$

$$
\begin{gathered}
{\left[\begin{array}{lll}
10 & 11 & 12 \\
13 & 14 & 15 \\
16 & 17 & 18
\end{array}\right]} \\
{\left[\begin{array}{lll}
1 & 2 & 3 \\
4 & 5 & 6 \\
7 & 8 & 9
\end{array}\right]\left[\begin{array}{ccc}
84 & 90 & 96 \\
201 & 216 & 231 \\
318 & 342 & 366
\end{array}\right]}
\end{gathered}
$$

threading


tieup

tieup





tieup


threading


## threading


frames per time step

threading

threading ("straight draw")

tieup
treadling
("straight treadling")


unique pattern rows = combinations of frames available (minus the useless ones)




# "network drafting" 


the original 1938 network drafting monograph: Brandon and Guiguet's Méthode des Initiales: Un aspect mathématique du tissage à lames


Olivier Masson \& Francois Roussel, 1988: Shaft Weaving and Graph Design

Anne Wells, 2000:<br>"Weavers Notes \& Guide" to Masson \& Roussel



Alice Schlein, 1994:<br>Network Drafting:<br>An Introduction



"any cloth structure which can be woven on an initial threading can also be woven on a threading plotted on its associated network."





"any cloth structure which can be woven on an initial threading can also be woven on a threading plotted on its associated network."









Schlein, page 46


Schlein, page 38

9. Threading from fig. 8 woven with an advancing twill treadling and twill tie-up.


Schlein, page 37






## Everyone gets a loom!


lealbaugh.github.io/little-loom/

lealbaugh.github.io/little-loom/

lealbaugh.github.io/little-loom/



Warp Lifting Plan of Weaving Calculated with Matrices
By Tadashi Fujita, Member, TMs,

Shiga Prefectural Junior College, Hikone, Shiga Pref.


## 1. Introduction

Attempts to systematize the structural designs of weaving mathematically have been made by T. Renaud [1], L. Lejeune and J. Soroge $[2]$, M. Tanaka [3], H.
Tsukiyama $[4]$, and T. Broggi $[5]$. Their works are all interesting as the basis of the theoretical development of the weaving designs.
In the conventional warp lifting plan, weaving
designs are filled with marks in the blank spaces of designs are filled with marks in the blank spaces of
design papers, the drawn-in draft and the treadling design papers, the drawn-in draft and the treading
are written down, and then the cording plan is built by tracing the marks of the designs, drawn-in draft
and treading. These procedures, however, are apt to cause
errors if the design is complicated. The author has developed a system to express the designs and the weaving plan by matrices to clarify the relation between them by the multiplication of these matrices, and to explain the characteristics of the lifting plan mathematically.
2. Relation Between Design and Cording Plan
2.1. Calculation of cording plan

Fig. 1 indicates the lifting plan of $\frac{2}{2}$ broken twill. Fig. 1 indicates the lifting plan of $\frac{2}{2}$ broken twill.
The weaving design is shown by A , the drawn-in by D . B , the treading by C and the cording plan in Assuming that $a_{t v}$ denotes the warp up mark whose elements are $a_{\text {a }}$ That is to say:

[^0]


[^0]:    

    Fig. 1 Lifting plan of $\frac{2}{2}$ broken twill
    
    a 0 an 0 or
    The element 0 of this matrix represents the weft
    p and the element $a_{t u}$ the warp up. The sub.index $k$ of the element represents the number of warp yarns counted from the left in one repeat; ; $i$, the number
    of weft yarns counted in reverse picking order. of weft yarns countee
    Assume that the points $■$ which warp yarn pa through the mail of heald at B are represented $b_{x}$ Then, the matrix of the drawn-in draft whose elements are $b_{t x}$ is as follows:

    $$
    \left(\begin{array}{cccc}
    0 & 0 & 0 & b_{14}  \tag{2}\\
    0 & b_{22} & 0 & 0 \\
    0 & 0 & 0 & 0 \\
    b_{41} & 0 & b_{33} & 0 \\
    0
    \end{array}\right.
    $$

    In this matrix, the sub-index $i$ of the element is
    the heald number; $k$, the warp number and mail the heald number; $k$, the war
    number having the same warp.
    Assume that the mark $\mathbb{C}$ in. C is represented by
    nes the element $C_{k}$ which indicates the matrix of tre

